# Interactive Planning for Autonomous Urban Driving in Adversarial Scenarios 

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#### Abstract

Autonomous urban driving among human-driven cars requires a holistic understanding of road rules, shortterm driver intents and long-term driving styles. This is a challenging task given the stochastic intents and driving styles of the road users. In addition, dynamically changing environments such as road intersections and traffic signals further increase the complexity. This paper presents an interactive behavior planning algorithm for adversarial scenarios in autonomous urban driving applications. Specifically, we propose a road context, driver intent, and driving style aware planner which infers beliefs over the latent states of surrounding exo-vehicles and uses a specialized Partially Observable Markov Decision Process to provide risk-averse decisions. We validate our proposed interactive behavior planner in simulation as well as on a full-size self-driving car. Our experimental results show that our algorithm enables safe and time-efficient autonomous driving even in adversarial scenarios.


## I. INTRODUCTION

Autonomous urban driving has been gaining popularity in recent years. A majority of research in this domain has an underlying assumption of exo-vehicles being driven by reasonably rational drivers. In this paper, we specifically focus on the adversarial scenarios for autonomous urban driving which are caused by irrational drivers. However, our proposed approach is applicable to complex driving scenarios with a combination of rational and irrational drivers. We achieve this with a holistic analysis of short-term driver intents and their long-term driving styles with respect to the contextual road rules for time-efficient and safe driving.

For example, consider the scenario that the ego-vehicle is driving on a street with two lanes and an exo-vehicle is driving in front. If the exo-vehicle intents to keep lane, the ego-vehicle can overtake by changing to the adjacent lane for efficiency. However, considering the intent alone sometimes leads the ego-vehicle to perform naive actions resulting in unforeseen outcomes. In addition to the driver intent, the egovehicle also needs to consider the driving style of the exovehicle. If the driving style of the exo-vehicle is aggressive steering, the ego-vehicle needs to keep a safe distance and change lane only when there is enough space in the lateral direction. Specifically, the intents of the exo-vehicles help the ego-vehicle anticipate their future actions so that it can make

[^0]time efficient decisions. Whereas, the driving styles help the ego-vehicle to stay at a safe distance from dangerous drivers.
The driver intents and driving styles of exo-vehicles are unfortunately, unknown to the ego-vehicle and need to be inferred. We infer the probability distributions over them for surrounding exo-vehicles using recurrent neural networks, based on their states and the road contextual information. The road context such as lane directions and distance to lane center can potentially help narrow down the space of possible driver intents and driving styles and in addition, speed up the planning process by filtering out invalid actions [1].

We propose, CID, Context, Intent, and Driving style aware planner which uses a Partially Observable Markov Decision Process (POMDP) framework to encode intents and driving styles as the hidden states, and simulate the possible future trajectories of neighboring exo-vehicles using the road context. We solve the POMDP using a risk-averse planner, ISDESPOT [2], to get the optimal action for the ego-vehicle. IS-DESPOT is a state-of-the-art online POMDP solver which applies importance sampling [3] to handle rare but critical events. We designed an importance function based on the driving styles, to handle collisions which are rare but critical events in autonomous driving. Our contributions in this paper are three folds: (a) an inference module for driving style analysis, (b) CID, an interactive behavior planner which integrates intent and driving style inferences with respect to road contextual information, (c) validation of our proposed CID planner using adversarial driving scenarios in simulation and on real-world data for qualitative analysis. We also validated our planner by comparing it to important baselines for quantitative analysis. Experimental results show that our planner can significantly outperform the baselines in terms of safety, especially for the adversarial scenarios, while achieving the same level of efficiency.

## II. RELATED WORK

## A. Driver Intent and Driving Style Inference

Driver intent and driving style inference has been studied intensively but independently. In [4], speed and lateral position changes are used for driving style detection. The work in [5] evaluates the Euclidean norm on accelerometer data and uses the deviations from the average of the norm to classify the driving styles using fuzzy logic. DrivingSense [6] classifies dangerous driving style based on smartphone autocalibration. The work in [7] uses linear regression to map a selected set of features to driving styles. These approaches normally divide driving styles into aggressive driving, normal driving, etc.. Our approach further divides them into
longitudinal and lateral styles to improve planning. A group of approaches [8], [9], [10] use HMMs or SVMs to predict vehicle's intents. Another group uses neural networks for intent prediction [11], [12], [13]. These approaches, however, require a huge amount of data for learning a range of intents. In contrast to the existing work, we leverage the road contexts for driver intent and driving style inferences and combine their outcome to obtain informative observations (e.g. right lane change with aggressive driving style) for interactive planning.

## B. Planning for Autonomous Driving

Driver intents and driving styles have been modelled independently for planning under uncertainty. For example, [14], [15], [16], [17], [18], [19] have modelled intents. MPDM [14] evaluates a fixed set of policies on the trajectories rolled out from the sampled intentions. However, it only plans for one-time interaction with other agents. IntentionPOMDP [15] modelled the autonomous driving problem as a POMDP to handle uncertain intentions. Luo et al. [16] improved on [15] by using an interactive motion model PORCA for the agents. However, both of them are designed for driving in pedestrian environments. The work in [19] has used a rich representation of road contexts to help predict vehicles' intention, but it also induces high computational complexity compared to our approach. Gao et al. [17] extract robot intent from a planned path and feed the intent to a neural network to generate robot vehicle control. However, their approach only considers the intent of the ego-vehicle, ignoring those of exo-vehicles. Driving styles have also been studied previously for planning under uncertainty in autonomous driving application. The work in [20] predicts vehicle's driving style: whether aggressive or patient. The predicted beliefs on driving style is modelled as hidden states in POMDP for autonomous driving. The work in [21] considers courteous driving style by placing a courtesy term in the cost function. However, the courtesy is only considered for the ego-vehicle. In contrast, our cost function considers driver intents and driving styles of exo-vehicles.

Our previous work [1] used only driver intent as the hidden states to formulate the autonomous driving problem as a POMDP. Like other existing work, it assumes drivers are rational with no adversarial behaviors. This paper focuses on adversarial driving scenarios caused by irrational drivers. We consider multiple exo-vehicles and use road contextual information for both driver intent and driving styles inference to achieve time efficient and safe decision making.

## III. Driver Intent and Driving Style Inference

We propose to use the road contextual information to help infer driver intents and driving styles of the exo-vehicles. The driver intent refers to actions such as, lane-keep and lane-change. Whereas, the driving style represents driving patterns that classify a driver as either rational or irrational driver based on the frequency of lane changes and brakes in their driving patterns. Our goal is to analyze and infer the driver intents and driving styles of other road users to
help in interactive, safe and time-efficient path planning for autonomous urban driving.

## A. Driver Intent Inference

We implement a Long Short Term Memory (LSTM) recurrent neural network for inferring the short-term driver intent beliefs of neighboring exo-vehicles [22]. We formalized the intent as the lane-keep, left-lane change or right-lane change. The input to the LSTM network are based on the geometric features derived from the vehicle trajectory and road contextual information. The features are (a) $\delta x$ : Change in lateral pose, (b) $\delta y$ : Change in longitudinal pose, (c) $l l$ : If left lane exists (Boolean $0 / 1$ ), (d) $r l$ : If right lane exists (Boolean 0/1) and (e) $d_{\text {center }}$ : Distance to the center of current lane. $d_{\text {center }}$ values range from $-1.5 m$ to $1.5 m$ as we consider average lane width to be 3 m . We train the LSTM network on sequences with 4 time steps of 0.25 seconds each. The training data for intent inference is obtained from NGSIM vehicle trajectory dataset [23] complemented with data collected by our ego-vehicle. The intent labels for the ego-vehicle data are marked by a safety driver using the indicator for referencing the start and the end of the intent.

## B. Driving Style Inference

The driving style inference is a critical aspect of autonomous safe planning which helps us in distinguishing a rational exo-vehicle driver from an irrational one for riskaware decision making. We define driving style according to the following categories: normal, longitudinally erratic, laterally erratic, and both (longitudinally and laterally) erratic. The decoupling of laterally and longitudinally erratic driving styles allows us to differentiate between the exovehicles that are aggressively steering and the ones that are recklessly accelerating and braking, respectively.

Consider a trajectory for an exo-vehicle which is defined as a temporal sequence of poses where a pose at time $t$ is represented as $\mathbf{p}_{t}=\left(x_{t}, y_{t}, \theta_{t}\right)$. We divide the driving trajectory into time intervals of 1 second comprising of 4 time-steps with equal time. We train another LSTM with the following features related to trajectory and road contextual information as inputs to the network: (a) $\delta x$ : Change in lateral position, (b) $\delta y$ : Change in longitudinal position and (c) $d_{\text {center }}$ : Distance to the center of current lane.

The aforementioned features were specifically selected as they efficiently represent the changes in the driving styles with respect to the road contextual information. The output of the LSTM network is a discrete probability vector $\phi_{t}$ over four driving style classes $\zeta$ : i.e., normal, longitudinally erratic, laterally erratic, and both (longitudinally and laterally) erratic which is provided every 0.25 seconds.

We trained the LSTM network for driving style inference on the NGSIM dataset. We extracted trajectories from the dataset and clustered them into discrete groups by comparing their deviation to candidate reference trajectories derived from our transition model as described in IV-B These clustered trajectories are then filtered and labelled by a human expert, before being divided into sub-sequences of 1 second.

We validated our proposed LSTM network by comparing it with a rule-based method and time series forest (TSF) [24], [25]. The rule-based approach considers the variance of $\delta x$ and $\delta y$ of the exo-vehicles and applies fixed thresholds to classify their driving styles. We use the same input features as LSTM for TSF, with default parameters except for the following: number of trees $=500$, maximum tree depth $=$ 10. We report the weighted average precision, recall and F1score for our test data in TABLE I Our proposed method outperforms TSF and rule-based method, as neural network based methods are robust to noisy and unbalanced data.

| Algorithm | Accuracy | Precision | Recall | F1 Score |
| :---: | :---: | :---: | :---: | :---: |
| Rule-based | 0.64 | 0.62 | 0.64 | 0.63 |
| TSF | 0.75 | 0.74 | 0.75 | 0.72 |
| LSTM network | $\mathbf{0 . 8 3}$ | $\mathbf{0 . 8 3}$ | $\mathbf{0 . 8 1}$ | $\mathbf{0 . 8 2}$ |

TABLE I: Classification report comparison
In scenarios where we can observe an exo-vehicle for a longer time period (longer than 1 second), we aggregate the past inferences by using a Bayes filter. The advantage of aggregating the inferences as compared to classifying a longer series of driving data is that it allows for a shorter lead time for the belief inference. From the classifier output $\phi_{t}$ at each time-step $t$, we use a multi-class discrete Bayes filter in the following recursive form to maintain a posterior class belief distribution of an exo-vehicle's driving style $\beta$ :

$$
\begin{equation*}
p\left(\zeta=\beta \mid \mathbf{p}_{1: t}\right) \propto \frac{p\left(\zeta=\beta \mid \mathbf{p}_{t}\right)}{p(\zeta=\beta)} p\left(\zeta=\beta \mid \mathbf{p}_{1: t-1}\right) \tag{1}
\end{equation*}
$$

where Bayes rule and Markovian assumption are applied. $p(\zeta=\beta)$ refers to the prior class distribution of predictions and $p\left(\zeta=\beta \mid \mathbf{p}_{t}\right)=\phi_{t, \beta}$, where $\phi_{t, \beta}$ is the output probability of the LSTM network corresponding to the class $\beta$ at time $t$. We also add a Laplacian smoothing factor in order to ensure $p(\zeta=\beta)>0$ for each class $\beta$.

## IV. Context, Intent and Driving Style Aware POMDP Planning

We formulate the behavior planning for autonomous driving as a POMDP [26] since it provides a principled way to model the uncertainty on intents and driving style for autonomous driving. We refer to our method as Context Intent and Driving style (CID) aware POMDP planner.

## A. POMDP Preliminary

A POMDP models an agent acting in a partially observable stochastic environment. It is formally defined as a tuple $\left(S, A, Z, T, O, R, b_{0}\right)$, where $S, A$, and $Z$ is the state space, action space, and observation space respectively. $T=p\left(s^{\prime} \mid s\right)$ is the probabilistic state transition from $s \in S$ to $s^{\prime} \in S$ when the agent takes the action $a \in A$. It models the imperfect control of the agent. $O=p(z \mid s, a)$ is the observation function defining the probability of observing $z \in Z$ when the agent takes $a$ and reaches $s$. This models the sensor noise. $R(s, a)$ is the reward function defining the reward the agent can get by executing $a$ when it at $s$. Since the agent does not know the exact state it is currently in due to partial observability, it maintains a belief, i.e., probability distribution, over its current state, and $b_{0}$ is its initial belief.

POMDP planning aims to find a policy $\pi$, a mapping from a belief $b$ to an action $a$, that maximizes the expected total discounted rewards:

$$
\begin{equation*}
V_{\pi}(b)=\mathbb{E}\left(\sum_{t=0}^{\infty} \gamma^{t} R\left(s_{t}, \pi\left(b_{t}\right)\right) \mid b_{0}=b\right) \tag{2}
\end{equation*}
$$

where $t$ is the time step, and $\gamma \in(0,1]$ is a discount factor which places preference for immediate rewards over future ones. The expectation is taken over the sequence of uncertain states and observations in the future.

## B. POMDP Model

1) State Modelling: The state in our problem consists of the road contexts $\Omega$, the pose $\mathbf{p}$ and the speed $v$ of each vehicle, the intent $\xi$ and the driving style $\beta$ of exo-vehicles.
2) Action Modelling: We define our action space as \{Lane-Keep, Left-Lane-Change, Right-Lane-Change\}. The steering and speed of the ego-vehicle is computed according to the planned action using our transition model.
3) Observation Modelling: The observation comprises the $\operatorname{road}$ context $\Omega$, the pose $\mathbf{p}$ and speed $v$ of each vehicle. To focus on modelling the hidden intent $\xi$ and driving style $\beta$, we assume the observation over $\Omega, \mathbf{p}$ and $v$ has no noise.
4) Transition Modelling: The transition function models the movements of each vehicle. We used a driving style enhanced Time-To-Collision (TTC) trajectory predictor to model the movements. Our predictor improves on our previous trajectory predictor [1]. The TTC trajectory predictor predicts the trajectory of a vehicle using 5th order and 4th order polynomial curve fitting for lateral displacement and longitudinal displacement, respectively. It uses a time-tocollision model to predict the end state. Specifically, it predict the end speed by

$$
\begin{equation*}
\dot{s}_{1}=\min \left(v_{\max }, \sqrt{\max \left(0, v_{\mathrm{f}}^{2}+2 a_{\max }\left(d_{\mathrm{f}}-d_{\mathrm{safe}}\right)\right.}\right) \tag{3}
\end{equation*}
$$

where $v_{\text {max }}$ is the maximum speed allowed, $v_{\mathrm{f}}$ is the current speed of the front vehicle and $d_{\text {safe }}$ is a predefined and fixed-value safe distance. The end acceleration is computed accordingly by

$$
\begin{equation*}
\ddot{s}_{1}=\left(\dot{s}_{1}-\dot{s}_{0}\right) / t_{1} . \tag{4}
\end{equation*}
$$

We improve on this TTC-based predictor by incorporating the driving style to it. Drivers with different driving style tend to keep different safe distances. Instead of using predefined and fixed-value $d_{\text {safe }}$, we adjust $d_{\text {safe }}$ based on the driving style inference of the surrounding vehicles. For example, we use a larger $d_{\text {safe }}$ for conservative drivers, to model its behavior of safe driving. In contrast, if a driver is aggressive, we use a smaller $d_{\text {safe }}$, to model its behavior of aggressive driving. With our driving style enhanced trajectory predictor, we build our transition function by adding a Gaussian noise on the trajectory. Specifically, for each time step, the transition of the pose is defined by:

$$
\begin{equation*}
p\left(\mathbf{p}_{t+1} \mid \mathbf{p}_{t-3: t}, \xi, \Omega\right)=f\left(\left\|\mathbf{p}_{t+1}-\mathbf{p}_{t+1}^{\mathrm{pred}}\right\| \mid 0, \sigma^{2}\right) \tag{5}
\end{equation*}
$$

where $\mathbf{p}_{t-3: t}$ is a 4-time-step history of the past poses, $\mathbf{p}_{t+1}^{\text {pred }}$ is the pose extracted from the trajectory predicted by our predictor, and $f$ is the probability density function of the Gaussian distribution with mean 0 and variance $\sigma^{2}$.
5) Reward Modelling: We designed the reward function considering both the time efficiency and the safety following the idea in [1]. We achieve time efficiency by penalizing the ego-vehicle when it drives on the lane farther to its destination by a penalty $R=-100 \times\left(d / d_{\max }\right)$ where $d$ is the distance from current lane to the destination lane and $d_{\text {max }}$ is the maximum inter-lane distance, and we penalize the ego-vehicle by a penalty $R=20 \times \frac{v-v_{\max }}{v_{\max }}$ to encourage it to select the lane on which it can drive faster. In addition, we penalize collisions with exo-vehicles with a penalty of $R=-1000 \times \max \left[(4-d)^{2}, 1\right]$, where $d<4$ meters is the distance between the two vehicles in collision. We sum them up with equal weights as the final reward.
6) Initial Beliefs: The initial beliefs over the intents and driving style at each time step is inferred by the intent and the driving style predictors as proposed in Section III.

## C. POMDP Solver

We use IS-DESPOT [2], a state-of-the-art online POMDP solver to solve our POMDP. To handle the high computational complexity of solving a POMDP, most state-of-theart online POMDP solvers leverages Monte Carlo sampling in planning. However, this naive sampling strategy often overlooks rare but critical events, resulting in risky policy. A key feature of IS-DESPOT is the use of importance sampling to handle rare but critical events. In autonomous driving, collisions are the rare but critical events. We use IS-DESPOT to handle collisions, generating risk-averse driving policies.

To use IS-DESPOT, it requires us to design an importance sampling distribution $q$, which, in this case, can be interpreted as a deformed transition function with increased probability for critical states and decreased probability for others. We design $q$ empirically. We increase the probability of the collision state for vehicles with erratic driving style.

## V. EXPERIMENTAL RESULTS

We validate our behavior planner CID, Context Intent and Driving style aware POMDP planner, with both simulated and real-world data. We compare the outcome of CID with different baseline algorithms as presented below.

## A. Baseline algorithms

We compared CID with five baselines, including, ReactiveController, SimmobilityST, Pessimistic-Planner, OptimisticPlanner and Max-Likelihood-Planner.

1) Reactive-Controller: Reactive-Controller [15] performs reactive actions based on ego-vehicle's distance to neighboring vehicles.
2) SimmobilityST: SimmobilityST [27] uses a hierarchical decision making process for controlling the driving behavior of each vehicle centrally.
3) Pessimistic-Planner: This is a variant of our CID planner with an assumption that all exo-vehicles are adversarial.
4) Optimistic-Planner: This is also a variant of our planner with an assumption that all exo-vehicles are rational. This assumption results in similar outcome to our previous work [1] where the driving styles of other road users is not accounted for planning.
5) Max-Likelihood-Planner: This planner plans vehicle actions assuming the world state to be the one that is the most likely inferred by our predictor. It plans by doing forward simulations starting from the current state and selects the action branch with highest reward.

## B. Experiments in Simulation

We used SimMobility simulator for exhaustively testing on a wide-range of scenarios with different intensities of adversarial behaviors for the exo-vehicles. The exo-vehicles are centrally controlled by SimMobilityST for normal driving styles and are modified for the erratic ones. The ego-vehicle is controlled by the corresponding baseline algorithm. We used real road network and the road contextual information for the simulations. For the qualitative analysis of our planner CID, we specifically designed five exemplar adversarial scenarios. Each of these scenarios present adversarial situations for the ego-vehicle's planner by executing either laterally or longitudinally erratic behaviors. These scenarios and their results from our planner are presented in Fig. 1

Scenario 1 (Fig. 1, Row 1) presents one slow moving, laterally erratic, exo-vehicle which constantly oscillates within the lane and frequently changes lanes. Without inferring the laterally erratic driving style of the exo-vehicle, the egovehicle can easily mistake it for a lane change intent and can potentially result in a collision. For example, OptimisticPlanner and SimmobilityST baseline algorithms expect a rational driving style from the exo-vehicle and attempts to overtake it, resulting in a collision. In contrast, CID accounts for the laterally erratic driving style of the exo-vehicle and slows down to maintain a safety distance.

Scenario 2 (Fig. 1, Row 2) generates one slow moving, longitudinally erratic vehicle that remains in lane but constantly brakes and randomly changes speed. This driving style of the exo-vehicle can potentially cause rear-end collision with ego-vehicle. Reactive-Controller is saved from the potential collision as it changes lane to increase its headway distance, however, it ends up in the lane which takes a longer path to the destination. SimmobilityST and PessimisticPlanner do not collide as they maintain a safe distance to the exo-vehicle though at the cost of taking a longer travel time to reach the destination. Optimistic-Planner attempts to overtake the exo-vehicle with the assumption that it would be rational and occasionally ends up in a collision when the exovehicle suddenly accelerates aggressively. Our planner, CID, infers the longitudinally erratic behavior of the slow moving exo-vehicle and changes lane. It then waits for a safety target gap and successfully overtakes the longitudinally erratic vehicle to align with the shortest path to the destination, thus accounting for both safety and time efficiency.

Scenario 3 (Fig. 1, Row 3) increases the adversity for the ego-vehicle with two longitudinally erratic vehicles in two lanes, providing only one option to avoid collision and reach the destination. Reactive-Controller surprisingly overtakes the first exo-vehicle however, with a very small safety margin. SimmobilityST and Pessimistic-Planner constantly follows the first exo-vehicle at a safe distance, taking a really
long time to reach the destination. Similar to Scenario 1, Optimistic-Planner attempts to overtake the first exo-vehicle with little gap between the two exo-vehicles and occasionally ends up in a collision due to a premature lane change. Our CID planner changes lane after inferring longitudinally erratic driving style of the first exo-vehicle. After changing lane, it finds the second vehicle and infers its behavior as longitudinally erratic as well, it then slows down and maintains safety distance to the second exo-vehicle until a gap is available for an overtake. It finally overtakes the first exo-vehicle and safely reaches the destination.

Scenario 4 (Fig. 1, Row 4) is a combination of two vehicles where the first one is longitudinally erratic and the second one is laterally erratic. Similar to Scenario 3, CID changes lane after inferring that the first exo-vehicle is longitudinally erratic. It then encounters the second exo-vehicle and infers that it is laterally erratic. Our planner then slows down and waits for a safe gap. Lastly, it waits for the second exo-vehicle to clear from the scene and increases its speed for continuing to the destination. Unlike our planner, all the other baselines except Pessimistic-Planner, occasionally results in a side-way collision with the laterally erratic exo-vehicle.

Scenario 5 (Fig. 1. Row 5) presents two laterally erratic exo-vehicles which eventually become normal. This scenario showcases the ability of our planner to dynamically update its actions while accounting for changes in behavior. Our CID planner first infers both exo-vehicles as erratic and slows down to keep a safe distance. Once the behavior of the first exo-vehicle is updated to normal, our planner passes it. Next, our planner then guides the ego-vehicle to stay in lane and keep a safe distance to the second exo-vehicle. Lastly, when the behaviour of the second exo-vehicle is also updated to normal, the ego-vehicle increases its speed and safely continues its path to the destination. All the other baselines except Pessimistic-Planner, occasionally result in a side-way collision with one of the laterally erratic exo-vehicles.

We randomly sample from adversarial scenarios to generate a range of adversarial driving sequences for quantitative analysis of our planner with respect to the baselines. We executed 100 iterations per algorithm. The performance criteria for the quantitative results is based on two fundamental metrics for autonomous driving: safety and efficiency. The safety is measured by collision rate and the efficiency by the travel time to the destination. A summary of our results for CID planner compared to the baselines in adversarial scenarios is presented in TABLE II

It can be observed that Pessimistic-Planner and our CID planner, both have zero collision rate. However, the Pessimistic-Planner takes longer travel time, showcasing poor efficiency. In contrast, CID has reasonable travel time compared to average travel time for all baselines. Both Optimistic-Planner and Max-Likelihood-Planner achieves better efficiency than our planner. However, they have higher collision rates because Optimistic-Planner believes all other drivers drive rationally while Max-Likelihood-Planner is too confident on the state it infers which, however, could be wrong. In addition, we also performed a comparative study

| Algorithm | Collision Rate | Travel Time (s) |
| :---: | :---: | :---: |
| Reactive-Controller | 0.21 | 61 |
| SimMobilityST | 0.21 | 74.5 |
| Pessimistic-Planner | 0 | 121.5 |
| Optimistic-Planner | 0.12 | 60.8 |
| Max-Likelihood-Planner | 0.17 | 62 |
| CID | 0 | 72 |

TABLE II: Adversarial Scenarios: Average performance comparison over 100 randomly generated scenarios.
when all exo-vehicles exhibit rational driving styles. The scenarios for the rational behavior are adapted from our previous work [1]. These results are presented in TABLE III.

| Algorithm | Collision Rate | Travel Time (s) |
| :---: | :---: | :---: |
| Reactive-Controller | 0.0 | 78.7 |
| SimMobilityST | 0.0 | 71.7 |
| Pessimistic-Planner | 0.0 | 162 |
| Optimistic-Planner | 0.0 | 63 |
| Max-Likelihood-Planner | 0.0 | 61.3 |
| CID | 0.0 | 63.2 |

TABLE III: Normal scenarios: Average performance comparison on 100 randomly generated scenarios.

Since all the exo-vehicles behave rationally, the collision rate is observed to be zero for all planners. In terms of efficiency, our planner performs at a same level as Max-Likelihood-Planner which has the least travel time.

## C. Experiments in Real World

We validated our planner using a self-driving car, SCOT [28] in a real urban environment of Singapore. We specifically tested Scenarios 1 and 2 with single exo-vehicle which is laterally and longitudinally erratic. The two scenarios are presented in Fig. 2 and 3 The high-level action of our CID planner is compared with the actions of an unbiased safety driver for the ego-vehicle who was not provided any information about the test scenarios. The speed of the egovehicle inferred by our transition model is also qualitatively compared with the human driver's decisions.

In Scenario 1, the vehicle initially infers the exo-vehicle as laterally erratic from its movement. CID outputs a lane keep action with slow speed to keep a safety distance. This action is in-line with the safety driver's decision. In frame 2 and 3, the exo-vehicle swerves between the two lanes, and CID outputs a right lane change action (indicated by red strip), while still keeping a slow speed, as the best option. Similarly, the safety driver decides to lane change. Finally, in frames 4 and 5, the exo-vehicle again attempts to block the ego-vehicle as an adversary. Both CID and the safety driver identifies the exo-vehicle to be lane-changing and maintains a safe speed in the current lane (blue strip).
For Scenario 2, frame 1, the ego-vehicle observes the exovehicle to be longitudinally erratic and maintains a safety distance while keeping in lane. In frame 2, CID outputs right lane change action. The safety driver also decides the same as seen in the following frame (frame 3). During frame 3, CID momentarily infers the exo-vehicle to be laterally erratic and slows down. It was observed that the safety driver had also slowed down. A potential reason is due to the fact that the exo-vehicle swayed towards right as

frame 1

frame 2

frame 3

frame 4

Fig. 1: Scenario 1 to 5 (row 1 to row 5), each with 4 frames. Ego-vehicle is in cyan. Exo-vehicles with normal, longitudinally erratic, and laterally erratic driving style are in violet, yellow and black stripes, and white and black stripes respectively. Actions are represented by blue, green and red lane strips for lane keep, left lane change and right lane change respectively.


Fig. 2: Scenario 1 in real world. The ego-vehicle (cyan) encountered a slowly-moving laterally erratic vehicle. The actions suggested by the planner matched with those the driver actually executed.


Fig. 3: Scenario 2 in real world. The ego-vehicle (cyan) encountered a slowly-moving longitudinally erratic vehicle. The actions suggested by the planner matched with those the driver actually executed.
there is an incoming merging lane on the left. In frames 4 and 5, our planner correctly infers the exo-vehicle to be longitudinally erratic (indicated as yellow) and accelerates in lane. The safety driver is also observed to increase speed while passing by the exo-vehicle. The online video (http: //bit.ly/cid_planner_2021) shows sample runs of CID both on the real car and in simulation.

## VI. DISCUSSION AND CONCLUSION

We presented a novel and interactive, context, intent and driving style aware POMDP planner, CID, for autonomous urban driving in adversarial scenarios. The road contextual
information and driver intent inference used for our planner helped in efficient planning, whereas the driving style inference accounted for safety. We validated our planner in challenging dynamic urban environments with adversarial scenarios. Our experimental results in simulation and on realworld data showcased significantly better performance of our planner compared to five different baseline algorithms.

## ACKNOWLEDGMENT

This research was supported by the National Research Foundation, Prime Minister's Office, Singapore, under its CREATE programme, Singapore-MIT Alliance for Research and Technology (SMART) Future Urban Mobility (FM) IRG.

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